allow a variation of 5.6 per cent. in either direction, or from -3.6 to +7.6 per cent., which renders the observation comparatively valueless. If, on the other hand, the number of the blind were 500,000, and those out of this number whose blindness was caused by smallpox were 2 per cent., or 10,000, the limits of error would only be 0.00056 in either direction, or 0.056 of one per cent.,

leaving a variation of 9,720 to 10,280 only.

Errors from Incomparability of Data.—The data to be compared should be strictly of a comparable nature.

The conclusion that a certain remedy is valuable in the treatment of some definite diseases is not demonstrated by the fact that the fatality in a series of cases thus treated is six per cent., while in another series treated without this remedy it is twelve per cent., unless it is shown that the ages and other previous conditions of the patients in the two cases are not widely different, and unless the numbers constituting the series are sufficiently great to avoid the fallacy due to paucity of data.

Errors from the Composition of Rates.—These are among the most common of all statistical errors, and show the fallacy of dealing with average rates by any shorter method than that of dealing with the sums of the num-

bers to be compared.

For example, the death rate of Boston in the census year 1900 was 20.81 per one thousand. That of Chelsea was 19.02, of Revere 14.14, and of Winthrop 7.59.

If these death rates are averaged as follows:

19.02 14.14 4)61.56 15.39

the resulting death rate of these four municipalities (Suffolk County) is 15.39, and very many instances are to be found in which this erroneous method is employed.

The only correct method of obtaining the combined

death rate is as follows:

Cities and towns.	Populations.	Deaths, 1900.		
Boston	560,892 34,072 10,395 6,058	11,671 648 147 46		
	611,417	12,512		

Therefore  $\frac{12,512 \times 1,000}{613,417} = 20.46$ , the true death rate of the County.

The error arises from the fact that the largest city in the group is given, in the first calculation, only as much prominence in obtaining the result as each of the others, namely, one-fourth of the whole, whereas its population constitutes over ninety-three per cent. of the whole.

Errors from Stating Deaths as a Ratio of the Total Deaths.—There is nothing erroneous per se in stating the deaths at any age as a percentage of the total number of deaths, or the deaths from any special cause as a percentage of the deaths from all causes. It is a useful and, in fact, the only method practicable when it becomes necessary to state the proportion of one of these to the other. But beyond this such method cannot be trusted. For example, the proportion of fatal accidents in Massachusetts, in 1900, among boys under five years of age was 14.5 per cent. of all fatal accidents among males, and that of girls of the same age was 24.3 of all fatal accidents of females. From these figures, however, it cannot be inferred that girls are more liable to fatal accidents than boys, since the contrary is the fact, the actual numbers being 205 such deaths among boys under five, and 126 among girls. The only reasonable conclusion is that at higher ages females are much less subject to fatal accidents than males. When stated as a ratio of the living

population of the same ages, the deaths by accident of boys under five were fourteen per ten thousand, and those of girls of the same age were only nine per ten thou-

Life Tables.—The usefulness of life tables is twofold. They constitute the basis of life insurance, and serve as an index of the sanitary condition of the community out of whose data they are constructed.

Life tables differ for the same group of population from year to year, and they also differ when calculated from the statistics of different portions of a group of inhabitants, as, for example, those of a large city, compared with those of any of the outlying districts beyond its

The work of constructing a life-table for any American State or city is necessarily less satisfactory in its results than the work of making a similar table for any of the civilized nations or communities of Europe, since most foreign populations are more stationary than those of

The essential data for constructing a life-table are the number, ages, and sexes of the living, and the same data

for the dying.

1. Theoretically, the best method of constructing a lifetable would be to observe a large number of children, all born on the same day, through life, entering in a column (headed  $l_x$ ) the number who remain alive at the end of each successive year, until all have died; and in a second colume  $(d_x)$  the number dying before the completion of each year of life. Therefore,  $d_x$  represents the number out of  $l_x$  persons, attaining the precise age x, who die before reaching the age x+1. Therefore  $d_x = l_x - l_x +$ 1, and the number dying between the ages x and x+1 is equal to the difference between the numbers living at the ages x and x+1. It is not practicable to observe a body of children throughout life in this manner, so that other methods must be adopted.

2. It is not necessary to assume, as in the preceding case, that all the persons have been born on the same day. If we could trace a large number of children throughout life, without reference to the dates of birth, a life-table could be constructed, if the number of the living and dying in each year of life were known.

The great life insurance companies employ a method somewhat similiar to this, in which tables are constructed from the results of watching a large number of insured lives from the time of insurance to death. These, how-ever, differ from the general population, in that they are selected lives, among whom unfavorable risks are weeded out by medical examination. The result of this process does not, however, present such striking differences from the general population as might at first sight be expected.

3. The common method of constructing a life table consists in taking the experience of several years and comparing the numbers of deaths of persons at different ages with the living at the same ages as determined by the census. For example, in the United States, and especially in States where reliable registration of births and deaths is made, the results of the decennial census enumerations may be employed together with the deaths occurring in the intervening years. By this means the disturbing effect of an epidemic year may be minimized. By this method results are obtained which, being wholly based upon recent observations, are more correct than if a million persons were observed from birth to death; since in the latter case the conditions which determined the rate of mortality might, before the whole series became available, have undergone very great changes, which for practical purposes would render the table valueless.

Dr. Farr's English life table No. 3 was based upon the

registered deaths in England during the seventeen years 1838-54, and on the two census enumerations of 1841 and 1851. Many other life tables of English cities and districts have been made since that time and were constructed upon similar principles.

The life table constructed by the writer upon the experience of the population of Massachusetts was based upon the deaths which occurred in the five years 189397, and upon the State census of 1895, the middle year of this period.

There are certain conditions which affect the accuracy of life tables, and particularly American life tables, which may be enumerated as follows:

1. The Influence of Migration.—The increase or decrease in the population depends upon two factors, migration and the difference between the numbers of births and deaths. In many of the States the gain by immigration is much greater than the gain by natural increase of births over deaths. Moreover, the increase by immigration is not uniform from year to year, nor is it equally distributed at the different age periods, fully one-half of the immigrants being between fifteen and thirty years of age, while the numbers at the extremes of life are comparatively small.

2. Defects of the Census. - Mr. H. Gannett, in a paper contributed to the American Statistical Association (Publications, vol. iv., p. 99) estimates a "shortage in the census of 1890 of negro children of about a quarter of a million," and of native white children "about the same." If this be correct, the entire shortage in the total population, including that of foreign whites, must leave a million unaccounted for in the United States. In States with complete registration it is possible to supply the deficiency for the first four or five years of life with a reasonable degree of accuracy from the registered births.

3. The Practice of Incorrectly Reporting the Ages of the Living and the Dead.—This error is of two kinds: (a) Greater numbers of persons are reported at the even ages, 20, 30, 40, etc. (both living and dead) than at 19, 21, 29, 31, etc., in consequence of the common habit of using round numbers instead of accurate ages. This may be partly eliminated by employing the periods 25–35,35–45, etc., instead of 20–30, 30–40, etc. (b) The habit especially among unmarried females of understating the ages of the living. This appears to a greater or less degree to be a common practice in all countries where census enumerations are taken.

4. Defects in Birth and Death Registration.—These defects depend upon the want of thoroughness with which the laws relating to birth and death registration are executed, and also upon the efficiency of such laws to secure the desired results. In some of the older States the birth and death returns are undoubtedly collected with a reasonable degree of completeness, and in such States life tables may be made from the returns of the whole popu

The following statement by Newsholme in the chapter on vital statistics in his "Hygiene and Public Health" presents in a condensed manner the general principles involved in the construction of a life table:

"It is usual to start with 1,000,000 or 100,000 children at birth and to make a separate table for the proportionate number of males and females at birth. Thus in Brighton in 1881–90 these were in the proportion of 51,195 × 48,805. Starting with 51,195 male infants at birth, and multiplying this number by .84608, the probability of surviving one year, we obtain 51,195 × .84608

> BRIGHTON LIFE TABLE. MALES. (Based on the mortality of the ten years 1881-90.)

Age.	Dying in each year of life. $d_x$ .	Born, and surviving at each age.	Sum of the number living, or years of life lived at each age, $x+1$ , and upward to the last age in the table. $\Sigma l_{x+1}$ .	Mean after life time (ex- pectation of
0	7.880	51,195	2,206,174	43.59
1	2,863	43,315	2,162,859	50.43
2	996	40,452	2,122,407	52.96
3	733	39 456	2,082,951	53.29
4	440	33,728	2,044,228	53.29
97	12	29	43	1.60
98	7	17	26	1.53
99	4	10	16	1.48

= 43,315. For the second year of life the probability of surviving was .93398; hence the number of survivors is  $43,315 \times .93398 = 40,452$ , etc. The general arrangement is shown in the preceding example of a life table, which only presents the data at or near the two extremes of life. the intermediate figures having been omitted from considerations of space.

The 43,315 males surviving to the end of the first year of life out of 51,195 born will each have lived a complete year in the first year, or among them 43,315 years. Similarly the 40,452 males will live among them 40,452 further complete years, and so on, until all the males started with become extinct at age 105. Evidently, therefore, the total number of complete years lived by the 51,195 males started with at birth will be  $43,315+40,452+39,456+38,723+\cdots+10+6+4+3+2+1=$ 2,206,174 years, this sum being obtained by adding together the numbers living at each age beyond the age in question down to its last item. This number of years is lived by 51,195 males. Hence the number of complete years lived by (i.e., the expectation of life of) each male 2,206,174

= 43.09 years. This is termed the curtate 51.195 expectation of life. It deals only with the complete years of life, not taking into account that portion of life time lived by each person in the year of his death, which may be assumed to be, on an average, half a year. Hence the complete expectation of life according to the above table is 43.59 years.

The materials for the construction of a life table are illustrated in the following table, from which the Massachusetts Life Table (1893-97), published in the Thirtieth Annual Report of the State Board of Health for 1898, was

POPULATION OF MASSACHUSETTS, 1885, AND DEATHS, 1893-97.

Ago nowled-	Popi	ULATION,	1895.	DEATHS, 1893-97.				
Age periods.	Total.	Males.	Females.	Total.	Males.	Fe- males		
0 to 5	* 235,647	* 118,453	* 117,194	78,779	42,710	36,069		
5 to 10	224,119	112,296		6,730	3,345	3,38		
10 to 15	202,900	101,574		3,460	1,655	1,80		
15 to 20	225,881	110,565		6,305	2,899	3,406		
20 to 25	265,983	123,692		9,982	4,899	5.08		
25 to 35	465,943	227,630	238,313	20,148	10,103	10.04		
35 to 45	341,535	168,997	172,538	18,832	9,610	9,22		
45 to 55	245.586	118,417	127,169	19.377	9,895	9,48		
55 to 65	157,651	72,766	84,885	22,334	11,278	11,056		
65 to 75	90,088	41,040	49.048	25,561	12,694	12,867		
75 to 85	35,405	15,460	19,945	20,547	9,675	10,872		
85 to 95	6,123	2,180	3,943	7,105	2,713	4,39		
Over 95	308	77	231	559	152	407		
Age unknown	3,014	1,554	1,460	496	378	118		
Total	2,500,183	1,214,701	1,285,482					

\*The population figures in this line (0-5) were not used in the construction of the life table, but the figures employed were estimated from the registered births and the deaths under five years of age.

In the English life tables it has been customary to estimate the population at the middle of a given year for life-table purposes, the census being taken on April 1st. In Massachusetts the census has usually been taken so near the middle of the year (about June 1st), that the slight error arising from the difference between this date and the middle of the year may practically be disregarded.

The deaths in any year are distributed throughout the year, and it is plain that the deaths registered at any age x will not have occurred at the precise age x, but some will have just attained that age, and others will have been close upon x + 1. Now it is assumed that these deaths at age x occur at equal intervals throughout the ensuing year, an assumption which is approximately correct except for the first two years of life. It is therefore customary to distribute the deaths in the first year of life by months, and then to calculate the mean from

## MASSACHUSETTS LIFE TABLE.

(Based on the Mortality of the Five Years 1893-97.)

		mahla M	o. 1.—Males.		ortality of	l the F	- Tears		. 2.—Female	8.	
Age.	Dying each year of age.	Born and surviving at each age.	Population : or years of life   lived in each year of age.	Years of life lived in and above each year of age.	Expectation of life at each year of age.	Age.	Dying in each year of age.	Born and surviving at each age.	Population or years of life lived in each year of age.	Years of life lived in and above each year of age.	Expectation of life at each year of age.
x.		and large	Para Property Propert	$Q_x$	Expe	x.	$-\frac{\mathbf{g}}{d_{x}}$	l <sub>x</sub> .	P <sub>x</sub> ·	$\frac{Q_{x}}{Q_{x}}$	$E_x$
0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 6 17 8 9 10 11 12 13 14 15 6 17 8 9 30 11 12 13 14 15 6 17 8 9 30 11 12 13 14 15 6 6 7 8 9 30 11 12 13 14 15 6 6 7 8 9 30 11 12 13 14 15 6 6 7 8 9 30 11 12 13 14 15 6 6 7 8 9 30 11 12 13 14 15 6 6 7 8 9 30 11 12 13 14 15 6 6 7 8 9 30 11 12 13 14 15 6 6 7 8 9 30 11 12 13 14 15 6 6 7 8 9 30 11 12 13 14 15 6 6 7 8 9 30 11 12 13 14 15 6 6 7 8 9 30 11 12 13 14 15 6 6 7 8 9 30 11 12 13 14 15 6 6 7 8 9 30 11 12 13 14 15 6 6 7 8 9 30 11 12 13 14 15 6 6 7 8 9 30 11 12 13 14 15 6 7 8 9 30 11 12 13 14 15 6 7 8 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9	8.849 1,794 818 559 424 816 252 205 170 146 123 110 111 135 181 195 181 195 208 289 296 301 305 309 313 316 319 320 325 328 331 316 319 320 325 328 331 341 346 348 352 359 368 379 368 389 379 361 379 388 389 398 410 429 448 466 468 552 5585 608 669 77 691 799 7729 7748 7789 789 789 789 789 789 789 789 789 7	51,350 42,501 40,707 38,889 38,389 38,389 38,389 38,389 38,389 38,389 38,389 38,389 38,389 38,183 37,817 37,684 37,389 37,284 37,785 36,894 36,692 35,786 35,288 36,692 36,686 35,288 34,829 34,633 34,829 34,633 34,027 33,718 33,403 33,087 32,769 32,450 33,118 31,481 31,484 30,836 30,171 29,834 29,147 28,795 28,436 28,068 27,296 26,457 26,009 25,543 25,060 26,457 26,009 25,543 27,296 26,457 26,009 25,543 27,296 26,457 26,009 25,543 27,296 26,457 26,009 27,296 26,457 26,009 27,296 28,436 28,436 28,436 27,296 28,437 28,068 27,498 28,438 29,147 28,795 28,436 28,438 29,147 28,795 28,436 28,438 29,147 28,795 28,436 28,438 29,147 28,795 28,436 28,438 29,147 28,795 28,436 28,438 29,147 28,795 28,436 28,438 29,447 28,795 28,436 28,438 28,438 28,439 28,438 28	46,343 41,604 40,298 33,609 33,118 38,464 38,235 38,484 38,235 37,532 37,753 37,639 37,753 37,639 37,753 37,154 36,583 36,375 36,141 35,683 35,683 35,673 34,781 35,583 35,673 34,781 33,560 33,245 32,928 32,920 31,971 31,650 31,326 31,000 30,670 30,338 32,928 32,920 31,971 31,650 31,326 31,000 30,670 30,338 32,609 32,900 31,971 31,650 31,266 31,000 30,670 30,338 32,615 32,928 32,930 32,911 31,650 31,326 31,000 30,670 30,338 32,615 32,928 32,911 31,650 31,326 31,000 30,670 30,338 32,615 32,928 32,911 31,650 31,326 31,000 30,670 30,338 32,615 32,920 31,971 31,650 31,326 31,000 30,670 30,338 32,615 32,920 31,971 31,650 31,326 31,000 30,670 30,338 32,011 31,326 31,000 30,670 30,338 32,011 31,326 31,000 30,670 30,338 31,000 30,670 30,338 31,071 31,050 31,326 31,000 31,000 31	2,263,907 2,217,564 2,175,969 2,135,662 2,096,033 2,018,187 2,056,935 2,018,187 1,979,723 1,941,488 1,903,440 1,865,550 1,827,795 1,941,488 1,903,440 1,775,2694 1,775,2694 1,775,2694 1,775,2694 1,775,2694 1,603,761 1,506,965 1,451,983 1,886,381 1,850,973 1,815,900 1,881,119 1,246,637 1,815,963 1,350,973 1,815,900 1,881,119 1,246,637 1,111,781,586 1,145,026 1,141,78,586 1,145,026 1,141,78,586 1,145,026 1,141,083,983 1,983,997 1,983,997 1,983,997 1,983,997 1,983,997 1,983,997 1,983,997 1,983,997 1,983,997 1,983,997 1,983,997 1,984,997 1,985,997 1,985,997 1,987 1,987 1,987 1,988 1,983	44.09 52.18 53.48 53.54 53.29 52.87 52.30 51.64 50.91 50.14 49.33 48.49 47.63 46.76 45.90 44.26 43.47 42.70 41.94 41.20 39.05 38.36 38.63	0 1 2 3 4 5 6 7 8 9 10 11 12 13 4 15 6 6 7 8 9 10 11 12 13 4 15 6 6 7 8 9 10 11 12 13 4 15 6 6 7 8 9 10 11 12 13 4 15 6 6 7 8 9 10 11 12 13 13 14 15 6 6 7 17 18 18 18 18 18 18 18 18 18 18 18 18 18	7,151 1,662 763 544 385 544 385 546 170 147 129 113 113 123 146 172 195 206 218 230 241 251 255 261 265 269 274 278 286 290 294 297 301 302 308 308 312 315 318 320 324 327 306 308 312 324 327 307 307 307 308 308 312 324 327 327 328 328 329 329 329 329 329 329 329 329 329 329	48,650 41,499 39,837 39,074 38,590 38,1457 37,577 37,371 37,201 37,054 36,925 36,812 36,639 36,258 36,639 36,258 36,639 35,499 35,168 34,917 34,662 35,499 35,168 34,917 34,662 35,499 35,168 31,565 33,897 33,593 33,163 33,897 33,1866 31,565 31,268	43,907 40,688 39,455 38,802 38,337 37,966 37,702 37,474 37,286 37,127 36,990 36,868 36,755 36,503 36,344 35,160 35,748 35,524 35,528 34,790 34,531 34,288 34,001 33,730 34,474 32,890 32,310 32,014 33,174 33,174 32,890 32,310 32,014 33,175 31,414 31,110 30,803 30,180 32,525 32,536 32,536 32,536 32,536 32,536 32,536 33,474 32,282 32,310 32,014 31,715 31,414 30,803 30,180 32,544 32,242 32,344 32,242 32,544 33,244 34,288 35,324 36,534 36,636 37,765 37,565 37,663	2.267,469 2.223,562 2.182,894 2.143,439 2.104,637 2.106,6300 2.028,314 1.990,612 1.953,138 1.915,552 1.871,735 1.804,877 1.768,112 1.731,475 1.694,972 1.658,628 1.632,468 1.632,688 1.747,948 1.744,966 1.773,161 1.737,3586 1.747,948 1.744,966 1.773,161 1.773,586 1.741,468 1.774,088 1.744,968 1.774,088 1.775,583 1.774,088 1.77	46.61 53.58 54.79 54.83 54.62 54.77 53.62 54.77 52.96 51.50 50.70 49.88 49.03 48.18 47.34 44.99 44.44 43.51 42.08 38.99 38.66 37.92 38.65 38.14 38.47 38.65 38.58 38.14 38.47 38.65 38.58 38.14 38.66

# Massachusetts Life Table.—Continued.

			_				The state of the s				
		Table N	o. 1.—Males					Table No	. 2.—Female	28.	
Age.	Dying in each year of age.	Born and surviving at each age.	Population or years of life lived in each year of age.	Years of life lived in and above each year of age.	Expectation of life at each year of age.	Age.	Dying in each year of age.	Born and surviving at each age.	Population or years of life lived in each year of age.	Years of life lived in and above each year of age.	Expectation of life at each year of age.
x.	$d_x$ .	$l_x$	$P_x$ .	$Q_x$ .	$E_x$ .	x.	$d_x$ .	$l_x$ .	$P_x$ .	$Q_x$ .	$E_x$ .
86 87 88 89 90 91 92 93 94 95 96 97 98	402 353 307 263 220 181 146 116 88 66 48 33 23 15	2,278 1,876 1,523 1,216 953 733 552 406 290 202 136 88 55 32	2,072 1,700 1,370 1,084 843 642 479 348 246 169 112 71 43 24	9,225 7,153 5,453 4,083 2,999 2,156 1,514 1,035 687 441 272 160 89 46	4.05 3.81 3.58 3.36 3.15 2.94 2.74 2.55 2.37 2.18 2.00 1.62 1.62	86 87 88 89 90 91 92 93 94 95 96 97 98	476 434 333 351 310 270 232 194 160 129 100 77 55 40 27	3,288 2,812 2,378 1,985 1,634 1,324 1,054 822 628 468 339 162 107 67	3,050 2,595 2,181 1,810 1,479 1,189 938 725 548 403 289 200 134 87 53	15,734 12,684 10,089 7,908 6,098 4,619 3,430 2,492 1,767 1,219 816 527 327 193 106	4.79 4.51 4.33 3.98 3.73 3.49 3.25 3.03 2.81 2.60 2.41 2.20 2.02 1.80

### MASSACHUSETTS LIFE TABLE.

Table No. 3.

(Based on the Mortality of the Five Years 1893-97.)

	m	x·	p <sub>1</sub>	x·	4-24 /0.44	m	x·	p	x·
Age.	ANNUAL M	IORTALITY	PROBA	BILITY	Age.	ANNUAL M	MORTALITY	PROBA	BILITY
		AT EACH		ONE YEAR	E Street History Bell	PER UNIT	AT EACH	OF LIVING	ONE YEAR
x.	YEAR C	OF AGE.	FROM EA	CH AGE.	x.	YEAR C	OF AGE.	FROM EA	CH AGE.
	Males.	Females.	Males.	Females.		Males.	Females.	Males.	Females.
0	0.19095	0.16287	0.82569	0.84939	51	0.01808	0.01596	0.98208	0.98417
1,	.04313	.04087	.95778	.95995	52	.01909	.01674	.98109 .97997	.98340
2	.02030	.01933	.97990 .98599	.98085 .98607	53	.02023	.01759 .01873	.97888	.98256 .98144
4	.01084	.01004	.98922	.99001	55	.02268	.01989	.97758	.98031
5	.00815	.00835	.99188	.99168	56	.02416	.02107	.97613	.97915
6	.00655	.00663	.99847	.99339	57	.02533	.02231	.97450	.97793
7	.00536	.00550	.99464 .99556	.99452	58	.02757	.02364	.97280	.97664
8	.00386	.00396	.99616	.99606	59	.02968	.02513	.96878	.97518 .97353
10	.00326	.00349	.99675	.99652	61	.03366	.02835	.96689	.97205
11	.00292	.00306	.99709	.99695	62	.03557	.03008	.96505	.97037
12	.00277	.00307	.99722	.99693	63	.03786	.03200	.96285	.96850
13	.00297	.00336	.99703 .99640	.99665 .99601	64	.04048	.03408	.96032 .95761	.96648 .96419
14	.00362	.00400	.99573	.99528	65	.04331	.03646	.95449	.96152
16	.00489	.00539	.99511	.99464	67	.05015	.04241	.95107	.95848
17	.00530	.00373	.99471	.99429	68	.05424	.04606	.94719	.95498
18	.00577	.00610	.99425	.99392	69	.05859	.05015	.94307	.95108
19	.00621	.00647	99381	.99356 .99320	70	.06325	.05434	.93869 .93430	.94710 .94301
2021	.00710	.00716	99292	.99286	71	.06794	.05866 .06327	.92951	.93867
22	.00752	.00733	.99251	.99268	73	.07834	.06788	.92466	.93435
23	.00792	.00756	.99212	.99249	74	.08385	.07273	.91953	.92983
24	.00824	.00773	.99179	.99230	75	.08979	.07784	.91407	.92508
25	.00851	.00791	.99153 .99131	.99212	76	.09586 .10252	.08312	.90852 .90248	.92020 .91500
26 27	.00892	.00831	.99112	.99170	78	.10984	.09458	.89588	.90969
28	.00912	.00850	.99092	.99154	79	.11740	.10075	88911	.90408
29	.00933	.00870	.99072	.99134	80	.12601	.10711	.88146	.89834
30	.00950	.00890	.99054	.99114	81	.13496	.11406	-87357	.89209
31 32	.00966	.00910	.99039 .99026	.99094 .99077	82	.14496	.12110	.86483 .85536	.88581 .87915
33	.00988	.00949	.99017	.99055	84	.16745	.13684	84549	87192
34	.01001	.00961	.99004	.99043	85	.18051	.14604	-83440	.86390
85	.01017	.00984	.98988	.99021	86	.19402	.15607	-82314	.85523
36	.01037	.01000	.98968	.99005	87	.20765	.16724	-81188	.84567
37 38	.01058	.01023	.98948 .98927	.98982 .98962	88,	.22409	.18019	.79850 .78356	.83470 .82322
89	.01101	.01063	.98905	.98942	90	.26097	20960	.76915	.81028
40	.01123	.01083	.98881	.98923	91	.28193	22708	.75290	.79607
41	.01150	.01109	.98857	.98897	92	.30480	.24733	-73551	.77989
42	.01180	.01128	.98827	.98878	93	.33333	.26759	-71430	.76399 .74522
43	.01215	.01152	.98792 .98753	.98855 .98831	94	.35772	.29197	.69655 .67324	72406
45	.01302	.01200	.98706	.98802	96	.42857	.34602	-64706	.70502
46	.01359	.01255	.98650	.98753	97	.46479	.38500	.62286	.67715
47	.01430	.01301	:98581	.98708	98	.53488	.41045	-57798	.65944
48	.01513	.01367	.98498	.98643	99	.62500	.45977	-52381	.62617
49	.01608	.01431	.98404 .98307	.98579	100	.69230	.50943	.48572	.00000
	.01100	.01014	.00001	.00100		NEW YORK		The state of the s	

Vital Statistics. Vital Statistics.

One hundred thousand infants, followed through their first year of life (in the period 1893-97) in Massachusetts, yielded 90,250 years of life. To obtain this mean of the infants living throughout the first year, the following method was employed:

All of the deaths of infants under one month old which occurred in the years 1893-97 were tabulated from the mortality returns in the office of the secretary of state, also those of infants who died in the second and the third months of life separately, then those of infants who died in the three succeeding months of life (fourth to sixth) in one group, and then those who died in the succeeding six months in another group. From these data, and from the births registered in the five years ending with June 30th, 1897, the figures for the first year of life were calculated after the method shown by Dr. Farr in his life table No. 3, page xxiii.

The foregoing mean, 90,250 (46,343 males and 43,907 females) (the arithmetical mean of the series  $l_0$ ,  $l_{12}$ ,  $l_{12}$ ,  $l_{13}$ , . . .  $l_1$ ), is used as the first term of column P (see foregoing table, p. 260). All of the succeeding terms in the column for the years 1, 2, 3, 4, etc., are the means of the terms in the preceding column  $l_x$ , using the formula,

$$P_x = \frac{l_x + l_{x+1}}{2}.$$

In these tables Column x presents the ages from birth up to one hundred years.

Column  $d_x$  presents the numbers of those dying in each age of life.

Column lx, Table 1, presents the survivors out of 51,350 males at birth at each age of life. (The females were 48,650, which added to the number of males makes 100,000.)

Column  $P_x$  presents the population maintained by the numbers in column  $l_x$ , beginning with 46,343 males (and 43,907 females), in all 90,250 persons.

Column  $Q_x$  shows the aggregate number of years which the persons at each age in the table will live, until their extinction by death.

Column  $E_x = \frac{Q_x}{L}$  is the mean future life time of the persons living at each age in the table, the expectation of life.

In the third table, the mortality column presents the mortality per unit of the population at each age of life, the figures being obtained by dividing the deaths at each age by population at such ages, the proper corrections and interpolations having been made, either by the analytical method described by Dr. Farr in his English Life Table, No. 3, p. xxv., or by the less accurate method known as the graphic method described by Mr. George King in the Journal of the Institute of Actuaries (October, 1883) and in Newsholme's "Vital Statistics," 3d edition, p. 266. From this column  $(m_x)$  the probability of living at each year of age  $(p_x)$  is obtained by the formula

 $\frac{2-m_x}{2+m_y}$  applied to each year of the series.

Column  $l_x$  is obtained by the formula  $l_x \times p_x = l_x + 1$ , and column  $P_x$  is obtained by the formula  $\frac{l_x + l_{x+1}}{l_x + l_x}$ .

From these tables it appears that, out of 100,000 children born alive in Massachusetts during the years 1893-97, 16,000 or nearly one-sixth die before arriving at the age of one year; 78,963 or nearly four-fifths attain the age of three years; 77,051 survive the age of five years, or seventy-seven per cent.; 50,124 or a little more than one-half attain the age of fifty-three years; 24,993 or nearly one-fourth live to the age of seventy-two years.

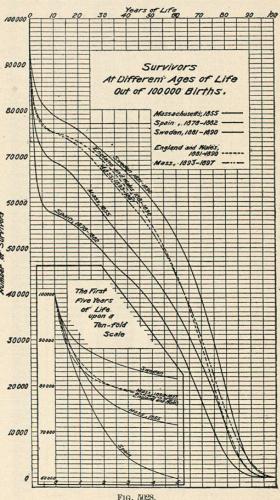
These figures present very decided differences as compared with those which were published for the same State in 1855 by Mr. E. B. Elliott.\* In that report it was shown that the numbers dying before the close of the first year out of 100,000 born were 15,510, or nearly the same as those for the year 1895 for the same age. At the

end of three years the survivors were only 74 per cent. instead of 79 per cent. as in 1895, and one-half had died before the close of the forty-first year, instead of surviving to the fifty-third as in 1895.

Since the numbers of each sex are unequal at birth, the males continue in greater numbers until the fifty-third year, when the greater death rate of the males has reduced their number below that of the females, and the females continue in excess throughout the remainder of life. Observing the tables more closely, it appears that the comparative intensity of the death rate of the sexes varies at different points of the table. For the first five years the death rate of males exceeds that of females. From age five to age nineteen inclusive the rate of females exceeds that of males, and from age twenty to the end of life the death rate of females is less than that of

In table 3 are presented two columns, in which are shown the probability of living one year from each age and the mortality per unit of the population at each year. At birth the probability of living a year is for males 0.82569 and for females 0.84939, that of boys at birth being about the same as for men of eighty-six, and that of girls about the same as that of women at eighty-six or eighty-seven. The probability of living a year is at its highest point for boys at age twelve (0.99722) and for girls it is about the same for age eleven as for age twelve 0.99695 and 0.99693).

A comparison of death rates at different periods presents certain points worthy of notice.



DEATH RATES AT DIFFERENT AGES OF LIFE, MASSACHUSETTS, AT crease in the number of years lived at the later ages of

Ages.	1865.	1895.	Ages.	1865.	1895.
All ages	20.64	19.0	30-40	11.7 11.9	9.7 12.6
Under 5 5-10	68.6 9.6	64.5	50-60	17.5 32.9	20.4 39.4
10-15 15-20	5.1 9.6	3.2 5.3	70-80 All over 80	70.5 168.2	82.4 184.6
20-30	12.6	7.1			

The death rate of children under five, and especially of those under one year of age, has not undergone very marked changes, but that of all ages from five to forty has very perceptibly diminished, while that of ages above forty has increased. This result has been produced by the great reduction in the number of deaths from infectious diseases, including consumption, which occur in the early period of life, from two years up to thirty. By this means a much larger ratio of the population than formerly survives to live throughout the useful and wage-earning period of life. This causes a material in-

These persons being spared from the diseases incident to childhood naturally increases the relative mortality from the diseases of adult life and old age.

This decided increase in the number of survivors throughout the useful ages of life has a marked effect upon the vitality of the population. It is undoubtedly due in no small degree to the increased attention which has everywhere been given in the past twenty-five years to public hygiene.

The accompanying diagram represents the numbers of survivors at the different ages of life in Sweden, England, Spain, and Massachusetts out of 10,000 at birth Those of Massachusetts are presented for two periods 1893–97 and 1855, showing the marked changes which have taken place. Sweden is selected because it has a low death rate and is often selected as a standard of a healthy population. Spain, on the contrary, has a high death rate, which is chiefly due to excessive mortality in the early years of life. (See table on p. 264 and diagram on p. 262.)

In consequence of the close contiguity of the lines in

PRINCIPAL VITAL STATISTICS OF THE SIX NEW ENGLAND STATES (FOR THE NINE YEARS 1892-1900).

Mean annual population of the period (estimated).	MAII 680,9		NE HAMPS 397,	SHIRE,	VERM 339,		MASS CHUSE 2,564,	TTS,	RHO ISLA 393,7	ND,	CONNECT 840,7	ricut,	TOTA NEW ENG 5,216,4	LAND,
	Num- ber.	Rate.	Num- ber.	Rate.	Num- ber.	Rate.	Num- ber.	Rate.	Num- ber.	Rate.	Num- ber.	Rate.	Num- ber.	Rate.
Marriages and rate per 1,000 population	49,706	8.11	35,385	9.90	25,481	8,45	205,738	8.91		8,72	1	7.81	406,319	NAME OF
population Deaths and rate per 1,000 popula- tion Deaths under one year and rate	127,954 100,334	20.88 16.37	73,554 64,419	20.58 18.02	62,904 50,716	20.61 16.62	630,798 434,604	27.33 18.83		26.02 19.00	- No.	23.48 17.46	1,165,110 849,579	
per 1,000 births	15,364 10,471	120.10 17.09	10,766 6,095	146,40 17,05	8,753 4,619	139.10 15.13	98,662 48,890	156.40 21.18		167,20 20,78	and the same	151.30 16.41	175,840 89,862	
Deaths from pneumonia, and rate per 10,000 population Deaths from typhoid fever, and rate per 10,000 population	9,029 2,015	14.73 3.29	6,273	17.54 2.78	5,091	16.68 3.12	43,252 6,242	18.74 2.70	6,279 1,025	17.72		15.41	81,588 1,354	
Deaths from smallpox, and rate per 10,000 population	5	.008	0	0	1	.003	65	.03	7	.02	26	.03	104	.02
10,000 population	331 367	.60	156 327	.44	172 278	.56	1,527 3,969	1.72		1.50		1.06	3,518 6,558	100
Deaths from diphtheria and croup, and rate per 10,000 population Deaths from cholera infantum, and rate per 10,000 population		2.58 8.17	1,035 3,597	2.89 10.06	970 1,626	3.18 5.33	12,765 22,520	5.53 9.76		5.06 12.57	Jel Keek	4.64 10.06	21,659 44,822	
Deaths from cancer, and rate per 10,000 population	4,470	7.29	2,430	6.80	2,001	6.56	15,532	6.73	2,188	6.17	4,328	5.72	30,949	6.59

#### INTERNATIONAL VITAL STATISTICS. Births per 1,000 of the Population in Certain Countries.

	England and Wales.	Scotland.	Ireland.	Den- mark.	Norway.	Sweden.	Austria.	Hungary.	Switzer- land.	German Empire.	Holland.	Belgium.	France.	Spain.	Italy.
Average of twenty-five years, 1875–1899	32.3 28.7	32.2 29.6	23.8 22.7	31.3 29.8	30.7 30.1	28.7 26.9	38.0	42.9 39.3	28.9 28.6	37.2 35.6	34.7 31.5	30,1 28.9	23.7 21.4	35.6 * 34.4	36.6 32.9
Death	s per	1,00	0 of	the P	opula	tion	in Ce	rtain	Coun	tries.					
Average of twenty-five years, 1875–1899	19.3 18.2	19.4 18.5	18.1 19.6	18.5 16.9	16.7 15.8	17.1 16.8	28.8	32.7 26.9	20.8 19.3	24.4 22.1	20.6 17.8	20.3 19.3	22.0 21.9	30.4 * 29.4	26.7 23.7
Marriage Ra	tes (1	900).	(Per	rsons	Marri	ied p	er 1,0	00 of	the	Popu	lation	.)			
1900	16.0	14.6	9.6	15.3	13.9	12.3		17.7	15 5	17.0	15.2	17.2	15.5	17.7	14.3

<sup>\*</sup> Spain, average of twelve years (1888-99).

the first five years of life, the figures for the first five years are given upon a separate diagram, in which the divisions representing the age periods are increased ten-

The preceding tables present the Vital Statistics of the six New England States, for the nine years 1892–1900. The populations which are given for each State, and for the whole district, are the mean annual populations of the nine-year period.

The Tables of International Vital Statistics contain the birth and death rates for the twenty-five years, 1875– '99, and for the year 1900, and the marriage-rates (persons married per 1,000 living) for the year 1900 in the principal countries of Europe.

DATA FOR CONSTRUCTION OF DIAGRAM OF SURVIVORS. TABLE SHOWING SURVIVORS AT DIFFERENT AGES OF LIFE OUT OF 10,000

BOR	N.			The second	Non-Ren
	Sweden-‡ 1881-90.	England and Wales—* 1881-90.	Massachu- setts— 1893-97.	Massachu- setts—† 1855.	Spain—‡ 1878-82.
0 1 2 3 4 10 15 20 25 30 35 40	10,000 8,895 8,586 8,399 8,258 7,882 7,713 7,551 7,338 7,109 6,876 6,628	10,000 8,536 8,067 7,878 7,758 7,495 7,423 7,281 7,090 6,844 6,550 6,216	10,000 8,400 8,054 7,896 7,786 7,516 7,394 7,213 6,959 6,674 6,372 6,054	10,000 8,449 7,733 7,424 7,258 6,873 6,726 6,487 6,100 5,748 5,408 5,078	10,000 8,083 7,060 6,433 6,151 5,747 5,602 5,413 5,164 4,908 4,596 4,378
45 50 55 60 65 70 75 80 85 90 95	6,349 6,043 5,687 5,239 4,658 3,900 2,948 1,872 894 275	5,839 5,405 4,891 4,275 3,534 2,684 1,786 970 388 100 14 .9	5,721 5,355 4,918 4,390 3,759 3,029 2,207 1,411 759 320 92 14	4,748 4,409 4,022 3,597 3,065 2,475 1,833 1,059 437 118 20.5 2,2	4,088 3,765 3,381 2,914 2,327 1,666 997 465 149 40

\*Fifty-fifth Report of Registrar-General, Supplement, vol. i., p. xiv.; vol. X., part i., p. 75.

+ Sixteenth Registration Report, Massachusetts, 1857.

+ Bulletin de l'institut international de statistique.

Samuel W. Abbott.

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VITILIGO.—This affection of the skin, which is likewise known by the name of leucoderma, consists in the development of whitened areas upon various portions of the body, but especially upon the face, neck, and hands. It is due to localized loss of pigment in rounded or ovoid patches of various size, having sharply defined margins and surrounded by more or less deeply pigmented skin which gradually shades off into the normal. The skin which gradually shades off into the normal. The characteristic features of the whitened spots are, that their border is usually convex, giving the impression that they extend into their darkened surroundings, or that, in their advance, they drive the pigment before them; that there is no change in the structure, sensations, or secretions of the affected areas; and that their tendency is to persist and to increase in extent, being little affected by any treat- including the hair and eyes, may be devoid of pigment.

ment. It is an acquired condition which comes on usually in youth or early adult life without previous ill health or prodromes, although in some instances it has been known to follow local injury; and sometimes it develops in the neighborhood of a pigmented mole. The dark-skinned races are rather more subject to vitiligo than those of fair skin and light hair, and it is not so very rarely seen in the negroes of this country, in whom the contrast be-

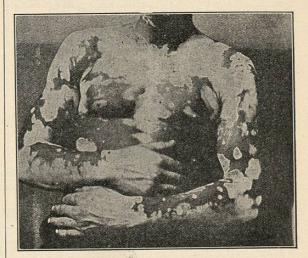


Fig. 5029 .- Vitiligo.

tween the perfectly white spots and the normal skin produces a striking effect. I have seen instances in which much discomfort of mind was occasioned by the fact that the white patches were merging into each other until extensive regions of the body had lost their pigment, and the negro was fearful that he was "turning into a white man." The hair may lose its pigment in the same way as the skin, and rounded or irregular tufts of gray may appear upon the head. In white races the affected regions are often more noticeable in the summer time, when the surrounding pigmentation becomes deeper

The diagnosis of vitiligo is not difficult, although it is liable to be confounded with morphœa, chloasma, tinea versicolor, syphilitic pigmentations, macular leprosy, and albinism. One chief point by which it is distin-guished from other conditions is the normal condition of the skin, apart from its loss of pigment. In morphœa there are structural changes. In tinea versicolor the patches are inflammatory and itchy, and from them there can be scraped scales which show, under the microscope, the characteristic groups of spores, although, when cir-cumscribed areas of healthy white skin are enclosed in the brownish patches of this disease, vitiligo may be closely simulated; but the margins will be found irregular instead of clean-cut. In chloasma there is increased pigmentation of the patch itself and the circumference is the part which appears white. The distinction has been made that in vitiligo the margin of the white area is convex toward that which is pigmented, while in chloasma it is concave; but in some instances the patches run together in such a way that this distinction becomes more theoretical than apparent. Syphilitic pigmentations, especially about the neck in women, may persist after other manifestations have disappeared and may, in some instances, be mistaken for vitiligo. In the macular form of lepra the patches of white skin have an irregular outline, not so abrupt as in vitiligo, and the tinge is rather grayish than dead white; then, too, the skin is either thickened or atrophied and anæsthesia or impaired sensa-tion is present. Finally, in albinism we have, as in vitiligo, an absence of normal pigment, but in the former it is a congenital defect and the whole surface of the body,

The pathology of vitiligo is obscure. Leloir has described a parenchymatous neuritis in which the axis cylinder had disappeared, the myelin sheath had broken down, and the nerve fibre had become transformed into an empty primitive sheath, whose nuclei had proliferated. The affection begins as a hyperpigmentation in areas which run into one another and assume a polycyclic character, the pigment becoming absorbed from the centre and deposited in excess in the marginal epidermis, the connective-tissue cells, and about the vessels and hair

The etiology of vitiligo is not well understood, but the cause of the condition is usually ascribed to perverted in nervation. It is probable that the disappearance of the pigment from one spot and its increased deposit in a neighboring part is due to atrophy in the former and to hypertrophy in the latter, both changes being effected through the agency of the sympathetic nervous system. Sometimes, though rarely, the proper proportion of pig mentation is spontaneously restored, but in the majority of instances the affected areas tend to increase in extent and the condition to assume marked chronicity. When large areas of surface are involved the term leucoderma becomes appropriate.

The treatment is unsatisfactory. Some reports of success from electricity have been made. Local applications for the removal of surrounding pigmentation are resorted to with the view of rendering the white regions less noticeable. The internal administration of nerve tonics, especially strychnine and arsenic, has been advised Blistering the patches to excite a deposit of pigment has been tried, but the results are not brilliant. If the spots are located upon the face or other exposed part, artificial staining may be employed, and dyes used to restore the color of the hair. Charles Warrenne Allen.

VITREOUS BODY OR HUMOR .- ANATOMY .- The vitreous body is a transparent, semifluid, colorless mass, of soft gelatinous consistence, subglobular in form, which fills the posterior four-fifths of the interior of the eyeball; it is bounded by the optic-nerve entrance and retina behind, by the retina on each side, and in front by the lens and its suspensory ligament which fit into a depression known as the patellar fossa. It serves as a support to the tunics of the eyeball, and, of lesser importance, as a clear refractive medium; its index of refraction is slightly greater than that of distilled water. Chemically, it consists of 98.5 per cent. water and 1.5 per cent. solids.

There has been much discussion regarding the structure of the vitreous. When the fresh substance is thrown upon a muslin filter, the greater part passes through as a watery liquid, a very small proportion remaining behind—demonstrating the existence of a supporting framework and a fluid portion. It is quite generally held that there is a very delicate fibrillar reticulum in which are scattered a few round or branched cells of the connective-tissue type, most abundant in the periphery, and often a variable number of migratory leucocytes. The cells are known as vitreous corpuscles; they are often difficult to recognize; they are peculiar in exhibiting large vacuoles which push the nucleus to one side, and in presenting a number of budlike swellings (Fig. 5030).

The vitreous body is enclosed in a delicate, structure-less, glassy membrane, the *hyaloid membrane*, which lies in close apposition with the entire inner surface of the retina; it can be readily separated from the latter, except posteriorly where the retinal vessels of fœtal life have entered, and anteriorly at the patellar fossa. At the ora serrata, the hyaloid membrane splits into two layers: the first, the hyaloid membrane proper, exceedingly delicate, which is continued over the anterior surface of the vitreous body; and the second, which blends with the posterior layer of the suspensory ligament of the lens.

The central portion of the vitreous body is penetrated by a channel (hyaloid canal, canal of Stilling, canal of Cloquet, central canal); this is filled with fluid, is limited by a wall of extremely delicate homogeneous membrane, and extends from the disc to the posterior pole of the

lens; it is about 2 mm. in diameter, with a slight dilata tion at both ends. This canal conveys the hyaloid branch of the central artery to the lens during feetal life; in the adult it forms part of the posterior lymph passages of the eyeball, having its outlet in the lymph spaces of the optic

The adult vitreous has no blood-vessels, its nourishment being received from the surrounding structures, particularly the uvea; hence diseases of the retina, choroid, and ciliary body almost always implicate the vitreous. Vitreous humor is never regenerated after oss; the diminution in volume is compensated for by the addition of aqueous. If the escape of vitreous is small, no injurious effects follow; if large, the consequences are serious—the globe softens, shrinkage results, and sight is lost.

#### DISEASES OF THE VITREOUS BODY.

Congenital Anomalies.—1. Persistent Hyaloid Artery.—During feetal life the hyaloid artery, a branch of the central artery of the retina, passes through the central canal of the vitreous from the optic-nerve entrance to the posterior pole of the lens; it usually begins to shrivel during the sixth month and has generally disappeared at the end of feetal life. Sometimes this process of obliteration fails, and a greater or lesser remnant of the artery persists during life. This can be seen with the ophthalmoscope as a grayish cord or thread which arises from the optic disc and stretches into the vitreous for a variable distance; it may terminate by a free extremity in the vitreous, or may traverse the latter and be attached to the posterior pole of the lens, the attachment to the lens being marked by a small opacity (congenital posterior polar cataract); or the thread may be attached to the lens with its free end floating in the vitreous; or the vestige may be represented by an irregular, minute deposit of connective tissue upon the disc. In rare instances the persistent artery continues to carry blood. Vision is generally good, but sometimes such eyes are

amblyopic or present other congenital defects.

2. Opacity of the Walls of the Hyaloid Canal.—In unusual instances the walls of the hyaloid canal are abnormally opaque, causing some interference with central acuteness of vision; this anomaly is visible with the ophthalmoscope as a grayish, tubular cord extending from

Hyalitis (Inflammation of the Vitreous).—This term includes two types: first, a purulent inflammation (sup-purative hyalitis), and second, a form characterized by the occurrence of opacities in the vitreous. As will be

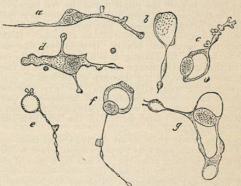


Fig. 5030.—Cells of the Vitreous Humor. (Schwalbe.) a and d without vacuoles; b, c, e, f, g, vacuolated.

readily understood by considering the avascular and almost structureless nature of this tissue, inflammations of the vitreous are rarely primary; they generally accompany or are the result of inflammation of the retina and